

# Solving Radical Equations Assignment

Solve the following radical equation.

1.  $\sqrt{x} = 3$

Checking solution:

2.  $2\sqrt{x} = 12$

Checking solution:

3.  $\sqrt{x} = 4$

Checking solution:

Solve the following radical equation.

4.  $\sqrt{x + 3} = 7$

Checking solution:

5.  $\sqrt{2y + 1} = 19$

Checking solution:

6.  $\sqrt{3x + 1} + 5 = 19$

Checking solution:

## Solving Radical Equations Assignment

7.  $x = \sqrt{x+2}$

Checking solution:

8.  $\sqrt{x-2} = 2-x$

Checking solution:

9.  $x-1 = \sqrt{5x-9}$

Checking solution:

Solve the following radical equation.

10.  $\sqrt{2x-1} + 5 = 2$

Checking solution:

11.  $\sqrt{2x+3} = \sqrt{x+2}$

Checking solution:

## Solving Radical Equations Assignment

12.  $\sqrt{11 - 2x} = \sqrt{x - 1}$

Checking solution:

13.  $2\sqrt{x + 8} = 3\sqrt{x - 2}$

Checking solution:

14.  $(4x + 1)^{\frac{1}{2}} + 2 = 5$

Checking solution:

15.  $x = \frac{\sqrt{10x + 3}}{5}$

Checking solution:

# Solving Radical Equations Assignment

## ANSWERS

Solve the following radical equation.

1.  $\sqrt{x} = 3$   
 $(\sqrt{x})^2 = 3^2$   
 $x = 9$

Checking solution:

$$x = 9$$
$$\sqrt{9} = 3$$
$$3 = 3$$

$x = 9$  is a solution of this equation  
 $\{9\}$

2.  $2\sqrt{x} = 12$   
 $(2\sqrt{x})^2 = 12^2$   
 $4x = 144$   
 $x = 36$

Checking solution:

$$x = 36$$
$$2\sqrt{36} = 12$$
$$12 = 12$$

$x = 36$  is a solution of this equation  
 $\{36\}$

3.  $\sqrt{x} = 4$   
 $(\sqrt{x})^2 = 4^2$   
 $x = 16$

Checking solution:

$$x = 16$$
$$\sqrt{16} = 4$$
$$4 = 4$$

$x = 16$  is a solution of this equation  
 $\{16\}$

Solve the following radical equation.

4.  $\sqrt{x+3} = 7$   
 $(\sqrt{x+3})^2 = 7^2$   
 $x+3 = 49$   
 $x+3 = 49$   
 $x = 46$

Checking solution:

$$x = 46$$
$$\sqrt{46+3} = 7$$
$$\sqrt{49} = 7$$
$$7 = 7$$

$x = 46$  is a solution of this equation  
 $\{46\}$

5.  $\sqrt{2y+1} = 19$   
 $(\sqrt{2y+1})^2 = 19^2$   
 $2y+1 = 361$   
 $2y = 361-1$   
 $2y = 360$   
 $y = 180$

Checking solution:

$$y = 180$$
$$\sqrt{2 * 180 + 1} = 19$$
$$\sqrt{361} = 19$$
$$19 = 19$$

$y = 180$  is a solution of this equation  
 $\{180\}$

# Solving Radical Equations Assignment

6.  $\sqrt{3x+1} + 5 = 19$   
 $\sqrt{3x+1} = 14$   
 $(\sqrt{3x+1})^2 = (14)^2$   
 $3x + 1 = 196$   
 $3x = 196 - 1$   
 $3x = 195$   
 $x = 65$

Checking solution:

$$x = 65$$

$$\sqrt{3 * 65 + 1} + 5 = 19$$

$$\sqrt{195 + 1} = 14$$

$$\sqrt{196} = 14$$

$$14 = 14$$

$x = 65$  is a solution of this equation

$\{65\}$

7.  $x = \sqrt{x+2}$   
 $x^2 = (\sqrt{x+2})^2$   
 $x^2 = x + 2$   
 $x^2 - x - 2 = 0$   
 $(x-2)(x+1) = 0$

$$x_1 = 2$$

$$x_2 = -1$$

Checking solution:

$$x_1 = 2$$

$$2 = \sqrt{2+2}$$

$$2 = \sqrt{4}$$

$$2 = 2$$

$x_1 = 2$  is a solution of this equation

$$x_2 = -1$$

$$-1 = \sqrt{-1+2}$$

$$-1 = \sqrt{1}$$

$$-1 \neq 1$$

$x_2 = -1$  is an extraneous solution of this equation

$\{2\}$

8.  $\sqrt{x-2} = 2 - x$   
 $(\sqrt{x-2})^2 = (2-x)^2$   
 $x - 2 = 4 - 4x + x^2$   
 $x^2 - 5x + 6 = 0$   
 $(x-2)(x-3) = 0$

$$x_1 = 2$$

$$x_2 = 3$$

Checking solution:

$$x_1 = 2$$

$$\sqrt{2-2} = 2-2$$

$$0 = 0$$

$x_1 = 2$  is a solution of this equation

$$x_2 = 3$$

$$\sqrt{3-2} = 2-3$$

$$1 \neq -1$$

$x_2 = 3$  is an extraneous solution of this equation

$\{2\}$

9.  $x - 1 = \sqrt{5x-9}$   
 $(x-1)^2 = (\sqrt{5x-9})^2$   
 $x^2 - 2x + 1 = 5x - 9$   
 $x^2 - 7x + 10 = 0$   
 $(x-5)(x-2) = 0$

$$x_1 = 5$$

$$x_2 = 2$$

Checking solution:

$$x_1 = 5$$

$$5 - 1 = \sqrt{5 * 5 - 9}$$

$$4 = \sqrt{16}$$

$$4 = 4$$

$x_1 = 5$  is a solution of this equation

$$x_2 = 2$$

$$2 - 1 = \sqrt{5 * 2 - 9}$$

$$1 = 1$$

$x_2 = 2$  is a solution of this equation

$\{5, 2\}$

# Solving Radical Equations Assignment

Solve the following radical equation.

10.  $\sqrt{2x-1} + 5 = 2$   
 $\sqrt{2x-1} = 2 - 5$   
 $\sqrt{2x-1} = -3$   
 $(\sqrt{2x-1})^2 = (-3)^2$   
 $2x - 1 = 9$   
 $2x = 10$   
 $x = 5$

Checking solution:

$x = 5$   
 $\sqrt{2 * 5 - 1} + 5 = 2$   
 $\sqrt{9} + 5 = 2$   
 $8 \neq 2$

$x = 5$  is an extraneous solution of this equation

$\emptyset$

11.  $\sqrt{2x+3} = \sqrt{x+2}$   
 $(\sqrt{2x+3})^2 = (\sqrt{x+2})^2$   
 $2x + 3 = x + 2$   
 $x = -1$

Checking solution:

$x = -1$   
 $\sqrt{2 * (-1) + 3} = \sqrt{-1 + 2}$   
 $\sqrt{(-2) + 3} = \sqrt{-1 + 2}$   
 $1 = 1$

$x = -1$  is a solution of this equation

$\{-1\}$

12.  $\sqrt{11-2x} = \sqrt{x-1}$   
 $(\sqrt{11-2x})^2 = (\sqrt{x-1})^2$   
 $11 - 2x = x - 1$   
 $3x = 12$   
 $x = 4$

Checking solution:

$x = 4$   
 $\sqrt{11 - 2 * 4} = \sqrt{4 - 1}$   
 $\sqrt{3} = \sqrt{3}$

$x = 4$  is a solution of this equation

$\{4\}$

13.  $2\sqrt{x+8} = 3\sqrt{x-2}$   
 $2^2(\sqrt{x+8})^2 = 3^2(\sqrt{x-2})^2$   
 $4(x+8) = 9(x-2)$   
 $4x + 32 = 9x - 18$   
 $5x = 50$   
 $x = 10$

Checking solution:

$x = 10$   
 $2\sqrt{10+8} = 3\sqrt{10-2}$   
 $2\sqrt{18} = 3\sqrt{8}$   
 $6\sqrt{2} = 6\sqrt{2}$

$x = 10$  is a solution of this equation

$\{10\}$

14.  $(4x+1)^{\frac{1}{2}} + 2 = 5$   
 $\sqrt{4x+1} = 5 - 2$   
 $\sqrt{4x+1} = 3$   
 $(\sqrt{4x+1})^2 = 3^2$   
 $4x + 1 = 9$   
 $4x = 8$   
 $x = 2$

Checking solution:

$x = 2$   
 $\sqrt{4 * 2 + 1} = 3$   
 $\sqrt{9} = 3$   
 $3 = 3$

$x = 2$  is a solution of this equation

$\{2\}$

**Solving Radical Equations** Assignment

15.

$$x = \frac{\sqrt{10x+3}}{5}$$

$$5x = \sqrt{10x+3}$$

$$(5x)^2 = (\sqrt{10x+3})^2$$

$$25x^2 = 10x + 3$$

$$25x^2 - 10x - 3 = 0$$

$$(5x-3)(5x+1) = 0$$

$$x_1 = \frac{3}{5}$$

$$x_2 = -\frac{1}{5}$$

Checking solution:

$$x_1 = \frac{3}{5}$$

$$\frac{3}{5} = \frac{\sqrt{10\left(\frac{3}{5}\right)+3}}{5}$$

$$\frac{3}{5} = \frac{3}{5}$$

$x_1 = \frac{3}{5}$  is a solution of this equation

$$x_2 = -\frac{1}{5}$$

$$-\frac{1}{5} = \frac{\sqrt{10\left(-\frac{1}{5}\right)+3}}{5}$$

$$-\frac{1}{5} \neq \frac{1}{5}$$

$x_2 = -\frac{1}{5}$  is an extraneous solution of this equation

$$\left\{\frac{3}{5}\right\}$$